## THE COMMODORE 64


by M.J. Winter


Explorations with the Turtle

The Commodore 64


by
M．J．Winter，Ph．D．

## Professor of Mathematics

Michigan State University

Illustrated by<br>Martin Cannon

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## (⿴囗) DATAMOST:

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For Elizabeth B. MacKenzie

## Acknowledgments

This is the third in a series of books written for young people (but not just for young people).

The first, Computer Playground, introduced BASIC through means of graphics, games, and words.

The second, Compumath Magic, showed those who already knew some BASIC how to use it to solve problems.

Now comes the LOGO Workbook, designed both to introduce the LOGO language and to teach how to use it in problem solving situations.

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# What is LOGO? 

## Why Learn It?

LOGO is called an educational language. It was designed for students, it is easy to begin using, and it is very powerful, i.e., it has the capability to do a lot of things. The educational value of learning LOGO, however, reaches far beyond the discipline of learning a programming language. A student learning LOGO will also learn:

- An increased understanding of geometry.
- Thinking processes and understanding of language.
- Problem solving techniques and the ability to handle multi-step problems.
- An appreciation of the power of recursion.

Two-thirds of the LOGO Workbook is directly concerned with geometric experiences. Students make the turtle draw pictures and designs. They investigate the effects of changes: does the box grow? will the pattern ever be complete? what happens if the angle gets smaller?, etc. The visual satisfaction of the turtle's drawings is a powerful motivation for investigation.

While using LOGO to draw boxes of different sizes, children will concretely experience the meaning of a variable. They will reinforce the concepts of points on a graph, and, of course, the measure of an angle. They will be able to investigate symmetry and the idea of a limit.

Problem solving skills are developed and applied at every level. To draw a house, one must first break down the problem into its
components: frame, roof, door, and window. When each piece or subprocedure has been solved, then one must put them together-synthesized into a greater whole.

Perceiving similarity among problems-"This is just like what we did but now the side is bigger"-leads to recursion, one of the most powerful mathematical and programming techniques available. Do it for this size, make the size bigger, do it again, keep going. . . .

Because the turtle's graphics are so delightful, many people neglect the word handling capabilities of LOGO. Yet the ability to manipulate words, sentences, and lists is essential to an understanding of grammar. LISP and the languages used in artificial intelligence work are all what are called "list processing languages," as is LOGO.

The last third of the Workbook deals with sentences and words. The applications are mainly in a "game" category. Children may be content with just doing the problems, or they may become intrigued enough to want to learn more.

Some aspects of LOGO have not been touched in the LOGO Workbook, which is after all, an introduction to the language. The mathematical commands-QUOTIENT, REMAINDER, ROUND, INTEGER-were not included. The purpose of the book is to teach LOGO through geometric applications and some list handling.

## LOGO and Young Children

(What to do before starting the workbook)
Many children will not immediately see the connection between saying FORWARD and seeing the turtle move up the television screen. Before using LOGO, young children should first "play turtle." Speak commands such as:

Forward 3 steps
Right turn
Forward 4 steps
Left turn
Forward 3 steps
Be sure they do not advance when told to turn.
Show them these paths. Ask them to choose which is the one they just made.


Lay out a 3 -segment path with masking tape, restricting the turns to right 90 degrees or left 90 degrees. At first, mark the steps on the tape. Have the children write out a set of directions
to travel the path. Blindfold a child and have her follow the directions. Did she walk the path?

A set of directions is called a procedure. Have the children write out directions to walk around a square or rectangle. Test the procedures using a blindfold.

Make the point that "right turn" and "left turn" refer to the child's right and left. In LOGO, they refer to the turtle's right and left.

On the LOGO Utility Disk that comes with the Commodore LOGO package is a program called INSTANT. This program uses single letter commands: R turns the turtle right 30 degrees, so that to make a square corner, RRR must be typed. This is an excellent introduction to LOGO for younger children.

## About the Workbook

## Using the Workbook With Different Age Groups

LOGO can be meaningful to different people in different ways. An 8-year-old will be pleased with teaching the turtle to draw designs. An older user will enjoy the designs, but will obtain even more satisfaction by understanding how to move the turtle on its "graph paper," thereby being able to draw solid figures and construct much more complex procedures. Not every lesson in the LOGO Workbook is for every user.

Suggested sequences of lessons are given below. The age groups are approximate, and offered as a guideline only.

| Ages | $8-9$ | $10-12$ | $13-? ?$ |
| :--- | :---: | :--- | :--- |
| Lessons | $0-11$ | $0-14$ | $0-3$ lightly |
|  | 27 | $17-20$ | $4-46$ |
|  | 29 | $22-24$ |  |
|  | $38-44$ | $26-29$ |  |
|  |  | $30-31$ (optional) |  |
|  |  | 35 |  |
|  |  | $38-45$ |  |

The first group includes the 3 rd and 4 th grades. The second group has some acquaintance with graphing on $\mathrm{x}, \mathrm{y}$-axes.
Classroom experiments have shown that 5th graders can do most of the lessons in the middle track. Beyond age 12, most children will have attained Piaget's level of variable understanding. They will understand and learn from the advanced lessons.

It is not necessary to complete each lesson before continuing, but the first two or three problems should be attempted. The final problems in many of the lessons are open-ended. These may challenge some users, as well as encourage individual exploration.

## List of LOGO Primitives

The words that LOGO recognizes without any "teaching" are officially called primitives. In the LOGO Workbook they are often referred to as commands. Below is a list of the primitives used in the book, and the lesson in which they first appear.

| Primitive | Long Form |  |
| :--- | :--- | :--- |
| DRAW |  | Lesson |
| FD |  |  |
| RT | FORWARD | 1 |
| LT | RIGHT | 1 |
| TO | LEFT | 1 |
| END | - | 1 |
| REPEAT | - | 4 |
| SAVE | - | 4 |
| READ | - | 4 |
| PC | PENCOLOR | 4 |
| BK | BACK | 5 |
| BG | BACKGROUND | 7 |
| DOUBLECOLOR | - | 7 |
| SINGLECOLOR | - | 7 |
| RANDOM | PRINT | 7 |
| PR | - | 7 |
| MAKE | HIDETURTLE | 10,20 |
| HT | SHOWTURTLE | 10 |
| ST | SETHEADING | 10,22 |
| SETH |  | 12 |
|  |  | 12 |


| Primitive | Long Form | Lesson |
| :---: | :---: | :---: |
| HEADING | - | 14 |
| IF | - | 14 |
| STOP | - | 14 |
| SETXY | - | 17 |
| HOME | - | 17 |
| RANDOMIZE | - | 20 |
| XCOR | - | 21 |
| YCOR | - | 21 |
| SETX | - | 21 |
| SETY | - | 21 |
| MAKE | - | 26 |
| RC | READCHARACTER | 29 |
| RC? | - | 29 |
| MEMBER? | - | 29 |
| ELSE | - | 29 |
| OP | OUTPUT | 35 |
| SQRT | - | 35 |
| COUNT | - | 38 |
| FIRST | - | 38 |
| BF | BUTFIRST | 38 |
| LAST | - | 38 |
| BL | BUTLAST | 38 |
| ITEM | - | 38 |
| WORD | - | 39 |
| SE | SENTENCE | 42 |
| LIST | - | 42 |
| RQ | REQUEST | 43 |
| TEST | - | 45 |
| IFT | IFTRUE | 45 |
| IFF | IFFALSE | 45 |
| ANYOF | - | 45 |
| ALLOF | - | 45 |
| POTS | PRINTOUT TITLES | APPENDIX |
| CATALOG | - | APPENDIX |

## Comments and Descriptions

Meet the Turtle is an introduction to the turtle and its movements. The connection between "a turtle" and the LOGO turtle is made by a sequence of drawings. All LOGO commands used here are repeated in Lesson 1.

Lesson 1 is designed to reinforce the idea of right and left turns. All turns are either LT 90 or RT 90.

Lesson 2 introduces turns of 120 and 135. The greater the turn, the sharper the angle drawn by the turtle.

Lesson 3 uses supplementary (adding to 180) angles. Try making a diamond using 160 and 20.

Lesson 4 introduces procedures. If each procedure is written on an index card, a convenient file can be assembled. Later, a student will be able to pull out the procedures needed for a particular lesson.

Lesson 5 is an exercise in visual problem solving. Students must first identify the components of each drawing, then experiment with the order used.

Lesson 6 illustrates how elaborate designs can be made by repeating simple shapes.

Lesson 7 defines BK and PC. Problem 5 requires planning ahead: deciding where to place the flowers, then deciding how to get there.

Lesson 8 introduces systematic variations. Problems 2 and 3 create different pictures by varying only one thing at a time. This systematic variation is a valuable problem solving technique.

Lesson 9 introduces variables. Problem 8 has two steps: first draw a picture in the box, then write a procedure to draw it on the screen. Other pictures might be a castle or cathedral.

Lesson 10 uses recursive procedures. Problem 4 is an exploration that can be extended. A turning angle of 144 draws a 5 -pointed star. In general, a figure with N sides will make N turns through angle A. The figure will be complete when the total of the angles turned through, NA, is a multiple of 360 .
$\mathrm{NA}=\mathrm{K}^{*} 360$
For a 5 -pointed star, $\mathrm{N}=5$, and the equation becomes
$\mathrm{A}=\mathrm{K} * 72$.
If $K=1$, then $A=72$ and the result is a pentagon.
If $K=2$, then $A=144$.
What happens if $\mathrm{K}=3$ ?
What A is needed for a 10 -pointed star?
Lesson 11 These drawings generate solid-looking figures. Problem 3 is a study of the effect of each variable.

Lesson 12 A regular polygon with a large number of sides looks like a circle. A circle with diameter D has circumference $\pi^{*} \mathrm{D}=$ $3.14 * \mathrm{D}$. A polygon with N sides, each side of length $3.14 * \mathrm{D} / \mathrm{N}$ will have the same circumference (perimeter).

The following all approximate a circle of diameter :DIAM
REPEAT 360 [FD :DIAM*3.14/36Ф RT 1]
REPEAT 180 [FD :DIAM*3.14/180 RT 2]
REPEAT 120 [FD :DIAM*3.14/12Ф RT 3]
REPEAT $90[F D: D I A M * 3.14 / 90$ RT 4]
REPEAT 72 [FD :DIAM*3.14/72 RT 5]

The product of the number of repeats times the angle is always 360.

Lesson 13 A review of arcs. The designs are pleasing.
Lesson 14 STOP ends the procedure PATTERN and goes back to PATT.

Lesson 15 PETAL repeats TINYARC RT 120 TINYARC three times. Different designs are produced from the basic pattern.

Lesson 16 This lesson is harder than it looks. The students must decide how to draw the tracks, then position and move the turtle.

Lesson 17 A review of $x, y$-coordinates may be necessary before starting this lesson. Many children are not familiar with the axes crossing in the middle of the graph paper.

Lesson 18 More complex pictures usually require orienting the turtle before each part is drawn.

Lesson 19 An open-ended, fun project. Some packages could be placed under the tree.

Lesson 20 To make LOGO think of a number from 1 to 6 , use:
$($ RANDOM 6$)+1$
Lesson 21 More on coordinates. Using SET is a fast way to draw lines.

Lesson 22 This lesson deals with recursive procedures that change the variable before calling themselves. :SIDE is the number that follows SHRSQ. If :SIDE was originally 100 , it becomes 90 , then 80 , then $70 \ldots$ decreasing by 10 each time SHRSQ is called. "Walk" students through this procedure.

Lesson 23 Fun with solid colors.

Lesson 24 More complicated drawings using SET. Problem 4 simulates animation.

Lesson 25 How to specify a circle by its center and radius. CIRCLE depended on the location and orientation of the turtle. RING does not.

Lesson 26 Practice in defining, or redefining, a variable.
Lesson 27 More recursive procedures-this time used for counting. How to count from 1 to 1000 .

Lesson 28 More practice with MAKE, this time in a drawing exercise. Encourage able students to form conjectures from the results of Problem 7.

Lesson 29 This is the first interaction with a running procedure. The line:

IF MEMBER? :ANS "AEIOU PR. . . . .
means, if :ANS is one of the letters of AEIOU then print. . .

Lesson 30 Filling in a solid by shading it as it is drawn. It may help to demonstrate the back-and-forth movement on the board.

Lesson 31 A problem solving activity. Students must decide the order in which the parts of each flag should be drawn.

Lessons 32, 33, 34 The special forwards defined in Lesson 32 are used recursively to produce interesting drawings and patterns. These lessons can lead to open-ended explorations.

Lesson 35 Handling subprocedures that are functions. SGN and ABS will be useful in Lessons 36 and 37. Outputs are referred to again in Lesson 45, but can be introduced there.

Lesson 36 An excursion into symmetry. Try bouncing off the "mirrors."

Lesson 37 Playing billiards with the turtle. This lesson does not depend on Lesson 36. The final corner depends on whether the (reduced) fraction $: \mathrm{L} /: \mathrm{W}$ is odd/odd, odd/even, or even/odd. When changing to a game of pool, use ABS to test when the ball is very close to a corner.

Lesson 38 An introduction to the word functions: COUNT, ITEM, FIRST, etc.

Lesson 39 Using the word functions from Lesson 38, many complicated tasks can be performed.

Lesson 40 The student is asked to write a more complicated procedure using words.

Lessons 41, 42 An introduction to lists, and lists of lists. In Lesson 41, BABBLE could be extended to include a list of adjectives. The resulting sentence would look like adjective, noun, verb, adjective, noun.

Lessons 43, 44 Giving words to a running LOGO procedure. In Lesson 43 , the procedure learns the names of animals. Lesson 44 is a "guess my number" game.

Lesson 45 uses TEST to decide whether to stop performing a recursive procedure. A test has an output-TRUE or FALSE. Use IFT and IFF to decide what to do next.

Lesson 46 The replacement procedure is a very elaborate combination of list functions, tests, and outputs. A student who doesn't understand its working (most won't) can still use it. The sequenced problems lead to a decoder to be used with an encoded message.

## LOGO on the Commodore 64

The LOGO package produced by Commodore is the full MIT LOGO, with enhancements made possible by the design of the computer. The built-in enhancements include:

1. Using the function keys to go to the text screen, split screen, or full screen at any time.
Pressing $\langle\mathrm{f} 1\rangle$ shows the text screen
<f 2) shows the split screen
(f 3$\rangle$ shows the full screen
These keys can be pressed at any time. The turtle will continue its activity without interruption.
2. From the Edit Mode, a procedure can be defined or saved by pressing the RUN/STOP key, as well as by the usual CTRL C.
3. The most recent line of commands is reprinted if the uparrow (needs shift) is pressed. The usual CTRL P also works.

Using the LOGO Utilities disk provided in the package enables LOGO to:
4. Print copies of the screen. This takes some time as the picture must first be saved, then the printing program loaded and run.
5. Use sprites. This provides ability to have eight turtles of different shapes, sizes and colors on the screen at one time. Each "turtle" can be controlled independently. The
sprites，however，do not physically rotate when told to turn，e．g．the butterfly always faces up no matter what direction it moves．

6．Play music，using the sophisticated sound available on the Commodore 64.

The $L O G O$ Workbook uses only the built－in features， $1-3$ ．

## Starting Up

The Commodore 64 LOGO package includes two disks：
－A LOGO utiltities disk．
－A LOGO disk．

To load LOGO：
－Turn on the computer and disk drive．
－Insert the LOGO disk．

- Type LOAD＂LOGO＂， 8 〈return〉．
- When READY appears，type RUN＜return〉．
－Wait about 3 minutes（may be less）．

When WELCOME TO LOGO！appears on the screen you are ready to begin．Remove the LOGO disk and store it safely．

If after 3 minutes，LOGO hasn＇t begun，turn off the computer and start again．

From Lesson 4 on，it is possible to save the procedures you write． To do this you must have prepared a formatted disk before loading LOGO．See Formatting a Disk in Appendix 2 of this book．


## Meet the Turtle



## From Log to LOGO

The LOGO turtle is a thin triangle. The sharp corner is its head; the larger end is where its tail would be.

Type DRAW and press $\langle$ return $\rangle$.
DRAW clears the screen puts the turtle in the center, headed toward the top.
FD 20 makes the turtle move forward 20 turtle steps.

# Type FD 20 〈return〉 <br> FD 60 〈return〉 

Where is the turtle now？Make an X in the box．

Try FD 250


Type DRAW 〈return〉．Try to find the exact number of turtle steps to reach the top of the screen．

It is about $\qquad$ steps to the top of the screen．

What happens if the turtle goes too far？

Type DRAW again．（Remember to press $\langle$ return $\rangle$ ．）
Then type：
RT 90
The turtle turned to its right．
Experiment：How many turtle steps does it take to get to the right edge of the screen？ steps．

Start with DRAW．Try to make the turtle draw this picture． All the turns are RT 90 s．
Write down everything you tell the turtle to do．

DRAW



## Lesson 1 Square Turns

All the turns in these problems are LT 90 or RT 90.
Each problem should begin with a clear screen for the turtle to draw on．Before starting each program type：

ND 〈return〉
DRAW 〈return〉
1．Type each line below and press $\langle$ return $\rangle$ ．
Watch the turtle move．
Copy the final picture in the box．

FD 30
RT 90 FD 30
RT 90 FD 30
LT 90 FD 20
2. Complete the program so the turtle draws a square.

FD 30
$\qquad$
3. Make the turtle draw a flight of stairs. Write your program here.

4. Make the turtle draw a plus sign.

Write your program here.

5. Make the turtle draw a skyscraper. Write your program here.



## Lesson 2 <br> Sharp Turns

These problems use turns of 120 and 135 to draw sharp corners.


1. Press $\langle$ return $\rangle$ after each line. Copy the final picture in the box.

FD 30
RT 120 FD 30
LT 120 FD 30
RT 120 FD 30
RT 120 FD 30

2. Using turns of 120 , draw a triangle.

Write your program here.
Begin with:
FD 30
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Copy the procedure and copy the final picture in the box.

FD 30
RT 135 FD 42
LT 135 FD 30
LT 135 FD 42

4. Using turns of 135, draw a triangle.

Write your program here.
Begin with:
FD 30
5. Draw the flag.

Write your program here.



## Lesson 3 Combined Turns

Diamonds can be made by combining turns of 120 and 60 , or by combining turns of 135 and 45.

1. Using turns of 60 and 120 , draw the parallelogram. The turtle begins at the point $T$.

FD 40
RT 60 FD 40

2. Make a parallelogram using turns of 45 and 135.

Write your program here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

3. Make a mountain ridge. Turn the turtle before beginning to move forward. Write your program here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

4. Draw a row of houses using turns of 45 and 90 . Write your program here.

5. Draw a glass.

Write your program here.



## Lesson 4 <br> Teaching the Turtle＊ Procedures and Repeat

In Lesson 1 you drew a box（or square）．To teach LOGO how to draw a box，type：

TO BOX 〈return〉
The screen will change to black．LOGO is now in the Edit Mode． TO BOX appears at the top．Type in these lines，pressing 〈return〉 after each line．

FD 30
RT 90 FD 30
RT 90 FD 30
RT 90 FD 30
END
If this is ok，press the RUN／STOP key．
If you need to correct something，read＂Comments about Editing＂ in Appendix 1.

Now type BOX 〈return）．
LOGO has learned a new command，BOX．

1．Erase the screen（with DRAW）．
Copy the drawing the turtle makes．
Type：

BOX BOX 〈return〉

2．Erase the screen，then type：

## REPEAT 4 ［BOX］

Copy the drawing．
When using REPEAT be sure to use brackets［ ］not parentheses．
3. Define two more procedures.
TO TRI1
FD 30
RT 120 FD 30
RT 120 FD 30
END
TO TRI2
FD 30
RT 135 FD 42
RT 135 FD 30
END

Press RUN/STOP to make LOGO accept the definitions. Then type either

```
TRI1 TRI1
or REPEAT 2 [TRI1]
```

How many repeats give you a complete picture? Copy the picture in the box.

REPEAT $\qquad$ [TRI1]
4. How many repeats with TRI2 give a complete picture? Copy the picture in the box.

REPEAT $\qquad$ [TRI2]
5. Define a procedure using the new procedures.

TO SUPERTRI
TRI1
TRI2
END
Experiment with
REPEAT $\qquad$ [SUPERTRI]

See if you can find out how many repeats of SUPERTRI make a complete design? $\qquad$ (This may be hard to tell.)
*If you have prepared a disk, you can save all these procedures for later use. Insert your personal disk and type:

## SAVE "FIRST.SHAPES

See Appendix 2, to learn how to format a disk, save procedures, and read in procedures.


## Lesson 5 Using Procedures

If you saved the procedures from Lesson 3, load your file by typing:

## READ "FIRST.SHAPES

Otherwise, type in the procedures BOX, TRI1, and TRI2.

1. What does this draw?

Copy the drawing in the box.
BOX
TRI2
TRI2
BOX
2. Put a turn before doing the steps in \#1, so that the house is right-side up.

Write your program here.
$\qquad$
3. Define a procedure STEP, which will draw this picture. STEP should begin

FD 30


Try to determine which combination of STEP, BOX, TRI1 and TRI2 produces each of these pictures.

Write your answers here.
4. $\qquad$

5. $\qquad$

$\qquad$
6. $\qquad$

$\qquad$
7.



## Lesson 6 <br> Super Procedures

Again you need BOX, TRI1, and STEP.
Superprocedures have procedures as commands. Writing a superprocedure makes changes easy to make, without a lot of retyping.

1. Define DESIGN

TO DESIGN
REPEAT 4 [BOX RT 20] END

Copy the drawing the turtle makes.
2. Now type EDIT DESIGN 〈return〉.

Change the 4 to 16:
Move the cursor on top of the 4, type 16.
You should now have the number 164 showing.
Move the cursor to the space beyond the 4, press the delete key and press RUN/STOP to define the new DESIGN. Consult Appendix 1, "Editing" if you have difficulty.

Try using different numbers of repeats. Record the two you like best.
3. Define PICT

TO PICT
REPEAT 3 [TRI1 FD 10 RT 60]
END

Run PICT, then change the number of repeats. How many repeats make a complete picture?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
4. Use TRI2 instead of TRI1 in PICT.

How many repeats will it take this time for a completed design?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
5. Experiment using some or all of your procedures in a superprocedure. Record at least one that makes an interesting design.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 7 Erasing and Retracing

These problems use BK, backward, and PC, pen color. BK is the opposite of FD.
PC is the color ink. If you type:
PC © the ink will be black.
PC 1 the ink will be white.
PC 2 the ink will be red.
etc.
If you type:
PC - 1 the pen is filled with ink eradicator.
Drawing over a line using PC -1 will erase the line.

1. Try this. Press $\langle$ return〉 after each line.

FD 50
PC - 1
BK 40
2. BK can be used to draw several lines radiating from one point. What does this draw?

TO MYSTERY
REPEAT 9 [FD 50 BK 50 RT 15] END
3. Use the same idea to define FLOWER.

Make the "petals" 20 units long.

4. Define STEM which draws a green stem under your flower. Then try FLOWER STEM.

TO STEM

Press $\langle f 5\rangle$ to show the picture on the full screen. Press $\langle\mathrm{f} 3\rangle$ to return to the split screen.
5. Write GARDEN which draws three flowers with stems, one red, one yellow and one blue.
Put in a green line for the ground.
Use PC -1 to move invisibly.
The first command in GARDEN will make the background white.

TO GARDEN
BG 1

6. Type DOUBLECOLOR GARDEN

The lines are now twice as thick.
Type SINGLECOLOR to get back to normal.
-


With PU (pen up) and PD (pen down) the turtle can move around without leaving a trail.

1. Try this.

TO KALEID
REPEAT 6 [TRI1 PU FD 30 RT 60 PD] END

Copy the drawing the turtle makes in the box.
2. Change the repeat to:

## REPEAT 6 [BOX TRI1 TRI1 PU FD 80 RT 60 PD]

Copy the drawing the turtle makes in the box.
3. Experiment! Change the repeat to each of these. Copy the drawing you like best in the box.

REPEAT 6 [BOX TRI1 TRI2 PU FD 80 RT 60 PD] REPEAT 6 [BOX TRI2 TRI2 PU FD 80 RT 6D PD] REPEAT 6 [BOX TRI2 TRI1 PU FD 80 RT 60 PD]
4. A halo is a FLOWER with the center half of the petals not drawn. Define HALO, making both the gap and the ray 20 units long.
$\qquad$
5. You can make another kind of blossom if you put a halo of one color around a flower of another color. (You might decide to give the outside HALO more rays, and a smaller angle.)

Your procedure should:

- turn the background white,
- select color,
- draw flower,
- change color,
- draw halo,
- make sure halo starts at edge of flower.

TO SUPERFLOWER
$\qquad$
$\qquad$
$\qquad$
$\qquad$



Lesson 9
Inputs Telling LOGO What Size You Want

A LOGO procedure can be told a number to work with. The procedure SQ will draw a square of any given size. SQ 10 will be a square with side $10 ; S \mathbb{C D}$ will be a square with side 80 .

To write SQ, type

TO SQ :SIDE (be sure to put a space after SQ)
:SIDE is a variable. When a variable is referred to, its name always begins with a colon.

TO SQ :SIDE
REPEAT 4 [FD :SIDE RT 90]
END

Run SQ 30. It looks the same as BOX, but something is different. If you don't see what it is, run:

SQ 30
SQ 30
and compare the picture with the result of BOX BOX in Lesson 4.

1. What does this draw?

SQ 10
SQ 20
SQ 30
2. What does this draw?

SQ 80
PU
FD 30 RT 90
FD 35
PD
SQ 10
3. Write a procedure that will make a face out of different squares.

$\qquad$
4. Here is a procedure that makes different triangles shaped like those made by TRI1.

TO TR :EDGE
REPEAT 3 [FD :EDGE RT 120] END

The picture drawn by TR 30 looks the same as TRI1, but the turtle turns a final corner.

Try:
TR 10
TR 20
TR 30
TR 40

Copy the picture. Then, without erasing, type:
RT 180
and repeat TR 10 TR 20 TR 30 TR 40
5. Write a procedure to draw this:
$\qquad$
6. Use TR, SQ (combined with invisible movement around the screen) to draw a house and garage.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

7. Write a procedure to draw the picture in the box. Be as efficient as you can!
$\qquad$

8. Draw a picture of a telescope or a rocket in the box. Write a procedure to make LOGO draw your picture.
$\qquad$
$\qquad$
$\qquad$


# Lesson 10 Endless Repeats 

If a procedure calls itself, it will repeat until you stop it by pressing CTRL G. A procedure which calls itself is a recursive procedure.

1. Try this.

TO ENDLESS<br>PRINT [FOREVER]<br>PRINT [AND EVER]<br>PRINT []<br>ENDLESS<br>END

The third PRINT prints a blank line.

Try to write procedures (you'll need more than one) that print.

## CLANCY LOWERED THE

BOOM BOOM BOOM
2. Try this.

TO FIGURE
RT 115
FD 100
FIGURE
END

Press $\langle f 5\rangle$ to see the entire screen.
3. A colored version of FIGURE uses a different color ink for each line.

TO FIGURE
RT 115
FD 100
MAKE "C RANDOM 9
PC :C
FIGURE
END

After a while the lines are so close that the computer does strange things with the colors.

You'll learn more about MAKE " in Lessons 22 and 26. You'll learn more about RANDOM in Lesson 20.
4. FIGURE drew a shape with side length 100 and turning angle 115.

PATTERN is like FIGURE except that both the side and angle are inputs.

TO PATTERN :SIDE :ANGLE
FD :SIDE
RT :ANGLE
PATTERN :SIDE :ANGLE END
(Try changing the pen color each time.)
What happens for each of these?


PATTERN 3060


PATTERN 3045


PATTERN 3090


PATTERN 55


PATTERN 11


PATTERN 40120


PATTERN 40135 PATTERN 40145

5．Try to find the angle that makes PATTERN draw a 5－pointed star．

6．Experiment with PATTERN．Try PATTERN 100ロ 300． Try PATTERN 500ロ 30ロ
Try other large numbers for the sides．
Try different angles．


## Lesson 11 <br> Donuts and Sugar Donuts

## (More Inputs and Recursions)

This project's goal is to draw a solid looking donut, sometimes with sugar sprinkles on it.

1. Write procedures to draw a hexagon and an octagon of variable sizes.

TO HEX :SIZE


## TO OCT :SIZE

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
2. DONUT will draw the hexagon, move a little, and draw it again.

TO DONUT :SIZE
HEX :SIZE
FD 12
RT 10
DONUT :SIZE
END

Try DONUT 3 and DONUT 10.
Change the move command in DONUT to FD 5 and try DONUT 10 again.

Change DONUT to use OCT instead of HEX.
Try DONUT 3 and DONUT 10 again.
3. It will be easier to experiment if you don't have to EDIT every time you want to change the distance moved and/or the angle. Rewrite the procedure DONUT so it takes three inputs: size, distance, and angle.
TO DONUT :SIZE :D :A
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Experiment until you can draw a large, solid-looking donut. Write down each try. Circle the ones that gave good results.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

What effect does each of these changes have on DONUT?
Changing the angle only? $\qquad$
Changing the distance only? $\qquad$
Changing the size only?


## Lesson 12 <br> Circles

You'll need procedures SQ and TR.
An octagon (eight sides) is rounder than a hexagon (six sides). To make a circle, we draw figures with even more sides - sometimes 180 sides, sometimes even 360 sides.

1. The procedure EYEBALL will draw 3 circles.
```
TO EYEBALL
REPEAT 360 [FD 1 RT 1]
PC }
REPEAT 180 [FD 1 RT 2]
PC 4
REPEAT 360 [FD 1.3 RT 1]
END
```

Copy the picture in the box. Draw a line from each REPEAT to the circle it generated.
2. To draw a circle of a given diameter (width) use:

TO CIRCLE :DIAM
HT
REPEAT 360 [FD :DIAM*3.14/36D RT 1]
ST
END
HT hides the turtle; ST shows the turtle. The turtle draws faster if it's hidden.

Try:
CIRCLE 40
CIRCLE 80
What is the largest the diameter can be before the circle goes off the screen at the top?
3. Write a procedure BIGCIRCLE to draw the largest possible circle on the screen. (The center will be at the middle of the screen.) BIGCIRCLE should move the turtle, then call CIRCLE.

TO BIGCIRCLE

$\qquad$
4. Try this program and copy the drawing in the box.

SQ 40 CIRCLE 40
5. Try:

CIRCLE 40
SQ 40

The procedures CIRCLE, SQ, and TR all return the turtle to the starting point, headed in the starting direction.
6. Write a procedure to draw each of these:

7. Write a procedure to draw a caterpillar.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 13 <br> Thirds of Circles

CIRCLE required 360 steps to complete．If only 120 steps are done，the result will be an arc which is one third of a circle．

1．Define the procedure ARC．

TO ARC ：DIAM
HT


REPEAT 120［FD ：DIAM＊3．14／360 RT 1］
ST END

Try：
ARC 50 〈return〉
ARC 5D 〈return〉
ARC 50 〈return〉
2. ARC can be used to make floral designs.

## TO FLORAL :S :A REPEAT 10D [ARC :S RT :A] END

Use CTRL G to stop the procedure when the picture is complete.

Try to copy the results of each of these. If it's too hard to copy, count the petals.


FLORAL 50180
FLORAL 100120


FLORAL 100135


FLORAL 10060


FLORAL 10090
3. FLORAL repeats unnecessarily; for specific examples, you can lower the number of repeats.

Make a flower arrangement with green leaves and at least one colored flower. Try to draw a vase or pot, too.

List your ARRANGEMENT procedure here.
Make a copy of your drawing.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


The turtle carries a compass and map with it. LOGO lets you use the compass in two ways.


HEADING tells the direction the turtle is heading. 0 is north (top of screen). Directions are in degrees clockwise from north.

SETH © aims the turtle in the direction of 0 (north). SETH stands for SET Heading.

SETH 90 aims the turtle toward 3 o'clock.

In both PATTERN and FLORAL the design is complete when the turtle is headed in the starting direction.

If you're going to use the compass, the starting heading has to be specified before PATTERN is called. Here's how:

```
TO PATT :S :A
SETH 0
PATTERN :S :A
PRINT [DONE]
END
TO PATTERN :SIDE :ANGLE
FD :SIDE
RT :ANGLE
IF HEADING = O STOP
PATTERN :SIDE :ANGLE
END
```

Try PATT 6075 and PATT 60 45
Write a starting procedure for FLORAL. Call it FLOW. Change
FLORAL so it stops when done.

1. Make a circle of stars. Your procedure will call PATT which will call PATTERN.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
2. Make a wreath of green leaves.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Try to put a wreath of green leaves both inside and outside a wreath of flowers.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 15 <br> Clover and Petals

FLORAL 100 120, in Lesson 13, produced a clover-like design. Define a procedure CLOVER to draw the design. CLOVER should not need any inputs.

TO CLOVER
REPEAT
END


Mark on the picture where the turtle is when CLOVER begins and ends.

1. Experiment with CLOVER. First try these, then find another pleasing design. Draw your results in the box.

REPEAT 5 [CLOVER RT 72]

REPEAT 8 [CLOVER RT 45]

REPEAT? [CLOVER RT 60]
4. PETAL draws the same design as CLOVER except the starting point is at the middle of the flower.

To write PETAL, you'll need TINYARC, which draws half of ARC 100.

TO TINYARC
REPEAT 6D [FD 314/360 RT 1]
END
Write PETAL. (What turns do you make?)
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
5. Write a procedure BLOSSOM to make a flower by spinning PETAL.
$\qquad$
$\qquad$


## Lesson 16 Keeping on Track

1. Write a procedure to draw the circular track and move the turtle around the track. The turtle should not leave a trail; it should keep going until CTRL $G$ is pressed.

The outer circle has diameter 150 .
The inner circle has diameter 120.

$\qquad$
$\qquad$
$\qquad$

There are several "tracks" shown on this page. Choose a track; then write a procedure to draw the track and then move the turtle around it.

Draw an arrow to the track you are using. Write your procedure here.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


# Lesson 17 <br> Setting Things Down 

The turtle is actually crawling over an invisible sheet of graph paper. When you type DRAW or HOME the turtle moves to the point in the center where the axes meet (the origin).


You can send the turtle to any point on the graph paper. The turtle will leave a trail.

Type DRAW. Then type each of these and watch the turtle.

SETXY 5090
SETXY 100 0
SETXY 50 30
SETXY © D
Copy what was drawn.

SETXY A B moves the turtle to the point (A,B). Unless the pen is up, a line is drawn.

1. Try this.
```
DRAW
PU
SETXY - 150 D
PD
SETXY © (- 125)
SETXY 150 0
SETXY © 125
SETXY - 150 0
```



The diamond touches the (invisible) edges of the LOGO screen.

Warning: If the second coordinate of the point is negative it must be enclosed in parentheses.
2. Using SETXY, write a procedure FRAME that frames the LOGO screen.

TO FRAME
$\qquad$
$\qquad$
$\qquad$
3. Use FRAME, SETXY, SQ, CIRCLE, PU and PD to draw the snowman. Add arms when you've got the rest of him.

TO SNOWMAN
$\qquad$
$\qquad$
$\qquad$
$\qquad$



# Lesson 18 Headings 

You'll need SQ and TR.


SETH is useful in turning the turtle before drawing a picture.

1. In HUT, SETH turns the turtle before drawing the roof.

TO HUT :SIZE
SQ :SIZE
FD :SIZE
SETH 30
TR :SIZE
END
Try HUT 60.

2. Before adding a door, you have the move the turtle. Add these lines to HUT.

SETH 180
FD :SIZE
LT 90
FD :SIZE/4
LT 90

Try HUT 60 again. Notice the direction of the turtle.
Add lines to draw a door. The height of the door should be :SIZE/2. The width should be :SIZE/4.

Add a doorknob, chimney, or window if you like. Remember to state all distances in terms of :SIZE.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Use HUT to draw a city street. Write your procedure here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 19 <br> Christmas Tree

You'll need the new version of PATTERN (Lesson 14) and TR.

Try this.

TO XMAS
PU
SETXY - 120 (-120)
PD
SETH 30
TR 240
PU
SETXY © ©
PD
SETH D
PATTERN 30115
END

Make some improvements:

- Change the background to green.
- Put a 5-pointed star on top.
- Add more ornaments, different colors and sizes.
- When the tree is all drawn, make the star on top blink (erase and redraw over and over).

Write your procedure here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 20 <br> Random

You'll need PATTERN and CIRCLE.

1. The LOGO command (it's called a primitive) RANDOM makes LOGO think of a whole number.

Type RANDOM 6 〈return〉.
To repeat this several times, press SHIFT and return. Repeat at least 10 times. What were the largest and smallest numbers to appear?
$\qquad$ largest.
$\qquad$ smallest.

RANDOM N gives a whole number between 0 and $\mathrm{N}-1$.

RANDOM 10 gives $0,1,2, \ldots$, or 9
RANDOM 4 gives $0,1,2$, or 3 .
(RANDOM 4) - 2 gives $-2,-1,0$, or 1
2. Try to draw a box using random sides.

TO RBOX REPEAT 4 [FD RANDOM 40 RT 90] END

Run RBOX a few times. Copy the craziest boxes.
3. Try a random pattern. Keep the angle at 60, but allow the side to range from 0 to 50 .

PATTERN RANDOM 50160
To move the pattern to a random place on the screen, we need a random x-coordinate between -150 and 150 , and a random ycoordinate between -125 and 125 .

Since the highest values may cause wrapping, we'll keep the x-coordinate between -140 and 140, and keep the y-coordinate between -100 and 100 .

```
TO SNOW
PU
SETXY (RANDOM 280)-140 (RANDOM 200)-100
PD
PATTERN RANDOM 50 160
END
```

To make a blizzard, turn SNOW into a recursive procedure.
TO SNOW
4. Write a recursive procedure BUBBLES. It should:

- Select a random spot on the screen.
- Select a random color ink (use PC RANDOM 9).
- Draw a circle of random diameter (up to 50).
- Call itself.

Turn the background white before you start.
Interesting things happen to the screen if this is left running for $5-10$ minutes. Copy your procedure here.

After this lesson, if you plan to use RANDOM, type:

RANDOMIZE 〈return〉
before you begin to work. Otherwise, you'll always get the same sequence of random numbers.


## Lesson 21 Pinetrees

Besides the compass, which keeps track both of the turtle's heading and true north, the turtle carries a map. You can use the map both to find out where on the invisible graph paper the turtle is sitting, and to move it.

XCOR is the x-coordinate of the turtle's position.
YCOR is the y-coordinate of the turtle's position.
SETXY A B moves the turtle to (A,B). SETX A
moves the turtle to (A,YCOR); only the xcoordinate is changed. This is useful when you want the turtle to move over.

SETY B moves the turtle to (XCOR,B). Used to move the turtle up or down.

1. PINETREE will make a tree with green branches and a brown trunk.

An outline of the procedure is:
TO PINETREE
start at top
SETH 220 BRANCHES
go to top
SETH 140
BRANCHES
TRUNK
END


BRANCHES draws a set of eight parallel lines:
TO BRANCHES
turn ink green
REPEAT 8 [FD ЗФ ВК ЗП SETY YCOR-8] END

Write out the full procedure PINETREE.
Also write the procedure for TRUNK.
TO PINETREE TO TRUNK
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
2. Make a forest of 20 trees. Select the tops at random, but be sure they are tall enough on the screen, but not high enough so the trees wrap around vertically.

Add a HUT for a country scene.

## TO FOREST

3. Write a procedure to draw an arrow with red top feathers and blue bottom feathers.

TO ARROW
$\qquad$
$\qquad$


## Lesson 22 Repeats With a Difference

Not only can LOGO procedures call themselves, but they also can change the inputs.

1. Define the procedure SHRSQ. SHRSQ is like SQ except for the next to last line, which shrinks the side by 10 before calling itself.
```
TO SHRSQ :SIDE
REPEAT 4 [FD :SIDE RT 90]
MAKE "SIDE :SIDE - 10
SHRSQ :SIDE -10
END
```

Run SHRSQ 60; stop with CTRL G when it begins to wrap around.

Look at what happened. First it drew squares of side 60, 50 40, . ., 10, 0, -10, - $20, \ldots$
$\mathrm{FD}-10$ is the same as BK 10 so the squares are drawn in the opposite direction.

Run SHRSQ 60 again. Let it go until there's no change. Copy the picture in the box.

To stop SHRSQ from calling itself forever, it should test the value of :SIDE.

TO SHRSQ :SIDE
REPEAT 4 [FD :SIDE RT 90]
IF :SIDE < © STOP
SHRSD :SIDE-10
END

Try SHRSQ 60 again. Then move the IF line to a better place.

Copy the final version of SHRSQ here.
$\qquad$
2. Write GRSQ, a procedure to enlarge a square up to side 100 . TO GRSQ :S
3. Change :SIDE -10 to :SIDE -1

Try SHRSQ again.
Try different colors.
4. Try to shrink and enlarge the triangles. Use SHTR and GRTR as names.

TO SHTR :S
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

TO GRTR :S
5. If SHTR and GRTR have no stopping test, do they eventually look the same?


1. If you were to build the hut in Lesson 18, using SHRSQ and SHTR from Lesson 22, you would have "painted" the hut.

Try to draw a hut with a solid red roof and blue walls.
List all procedures (including SHTR and SHRSQ) here.
If possible, draw a street of different colored, different sized huts.
2. Draw a patchwork quilt of solid squares. The squares should all be side 60 , but their colors and locations should be random.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 24 Using Set to Draw

LOGO draws faster if the turtle is hidden. It draws much faster if straight lines are drawn using SETXY rather than FD.

1. SETSQ draws a square with side twice the input. The center of the square is the HOME position. Try to figure out how the square will be drawn, before trying the program.

TO SETSQ :S
PU HT
SETXY :S :S
PD
SETY -:S
SETX -:S
SETY :S
SETX :S
END
Copy the square. Number the sides in the order they are drawn.
2. Because SET is faster than FD, and because it doesn't retrace lines, SETSQ will make a solid-color square much faster than SHRSQ. Write a procedure to make a solid square using SETSQ. Try SOLSQ 30.

TO SOLSQ :S
3. SETSQ is limited to a square centered at the origin. Make a succession of solid squares, largest one first, in random colors to get a quilt pattern. Decrease :T by 10 each time MASTER is called:

TO MASTER :T

4. Without the recursion, SETSQ draws one square at a time. Delete the recursion line from SETSQ. A procedure that erases a square before drawing the next smaller one will make it look as if the square is shrinking.

TO SHRINK :N
IF : N < 1 STOP
PC -1
SETSQ :N+1
PC 7
SETSQ :N
MAKE "N :N-1
SHRINK :N
END
5. Write a procedure BLAST, that is the opposite of SHRINK. BLAST starts with a small square, which appears to become larger and larger.

TO BLAST


## Lesson 25 <br> Rings

You'll need CIRCLE from Lesson 12.
Sometimes it is more convenient to specify a circle by its center and radius. That way, LOGO will always draw the same circle, no matter which direction the turtle is heading.

RING takes three inputs, the coordinates of the center and the radius.

TO RING :XCEN :YCEN :RAD
PU
SETXY :XCEN :YCEN
FD :RAD
RT 90
PD
CIRCLE 2*:RAD
END

1. Use RING to make a nest of four circles. Each should have a radius 10 more than the last. Draw the smallest circle first. Write your procedure here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
2. Go the other way: draw nested circles, the largest first. Reduce the radius by 10 each time. Keep going until the radius is $<1$. Write your procedure here.
3. Write a procedure to shrink and blast circles.
4. Try to draw a solid circle by using the procedure from problem 2 with each radius 1 less than the previous one.
5. Draw a target with each band a different, solid color. The radius of each band is 10 more than the radius of the band inside it. Go to six bands.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 26 <br> Defining Variables

You'll need SQ from Lesson 9.
When a variable is used in a LOGO procedure its name is preceded by a colon.

Examples: :SIZE :EDGE :ANGLE
When a procedure defines a variable, MAKE " is used.
Examples: MAKE "X 6 MAKE "N 2*:X

1. Try this one.

MAKE "DOG 50 SQ :DOG MAKE "HELLO [HI THERE]
PR :HELLO
PR [HELLO]
2. Write a procedure SUM which has two inputs, :X and :Y. SUM defines a new variable $: S$ to be the sum of $: X$ and $: Y$. After defining :S, SUM should print it.

TO SUM :X :Y
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. MAKE " is used when you want to change the value of a variable during a procedure. DEMO doubles :N.

TO DEMO
MAKE "N 4D
PR : N
MAKE "N 2*:N
PR :N
END
4. Change $D E M D$ so that instead of printing $: N$ each time, it draws SQ :N.
$\qquad$
5. NESTS is a procedure which calls itself, but changes : N every time.

TO NESTS :N
IF $: N=\mathbb{D}$ STOP
SQ :N
MAKE "N : N -10
NESTS :N
END

See if you can predict what NESTS 80 will do.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
6. Before NESTS calls itself again, move the turtle. Insert these lines before NESTS :N.

FD 10
RT 90
FD 10


## Lesson 27 <br> Keep Counting

The procedure COUNTER will keep going until CTRL G is pressed.

TO COUNTER :N<br>PR :N<br>MAKE "N : $\mathrm{N}+1$<br>COUNTER :N<br>END

Try COUNTER 1.
Change COUNTER so it counts by fives:
2. To make COUNTER stop, put in a test:
IF :N > 100 STOP

Rewrite COUNTER to count to 1000 by 3 s .
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Define BLASTOFF. It should count from 10 to 0. Pause between each number (use REPEAT 50D [ ] to make it do nothing 500 times).

When the count reaches 0 , something fancy should happen. Change the screen color several times.

Record your final BLASTOFF procedure-and any procedures it uses.
4. Write a reaction tester. Tell the user to be ready to press CTRL G when the numbers appear.

Use a pause of random length before printing the numbers.
Write your procedure here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 28 <br> Spirals \& Angle Spirals

SPIRAL is like PATTERN (Lesson 10), except that each time the turtle turns, the side gets bigger.

The inputs are :A the turning angle and :R the number of repeats.

The length of the side, $: S$, is a variable. When $: S$ is given a value or changed, MAKE "S is used.

The procedure SPIRAL is:
TO SPIRAL :A:R
MAKE "S 1
REPEAT :R [FD :S RT :A MAKE "S :S+2]
END
(Use CTRL G to stop SPIRAL.)

1. Some spirals look, at first glance, like polygons. Try these inputs for SPIRAL:

A R Looks like a
12050
14450
$90 \quad 50$
16050
2. If the angle is changed slightly from a "regular polygon" spiral, the result looks like a spiral galaxy.

Try these. Copy the curved lines that seem to appear.
SPIRAL 14568

SPIRAL 9160
3. Write a procedure UNSPIRAL which is like PATTERN, except that the angle increases by 5 each time the turtle turns.

## TO UNSPIRAL :S :R

4. Try UNSPIRAL 10300.

Copy the picture in the box.
5. Change the amount the angle increases to 6. Try UNSPIRAL 10300 again.
Copy the picture in the box.
6. Since changing from 5 to 6 made such a difference, rewrite UNSPIRAL so the angle increase :AI is an input.

TO UNSPIRAL :S :R :AI
7. Try angle increases of $2,4,8,9,10$, at least. Start with side 10 and 1000 repeats. You may have to use a smaller side and/or use SETXY at the beginning to fit the unspiral on the screen.

Copy the pictures here. Record the side length, angle increase, and any other changes you made under each picture.

$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 29 Pressing a Key

You'll need MASTER and SETSQ.
You can ask LOGO whether a key is being pressed, and you can tell LOGO to wait until a key is pressed.

RC or READCHARACTER means wait until a key is pressed.
Then RC will have the value of the key which was pressed.
Here are two examples of using RC:

1. Define FLASHY and run it.

TO FLASHY
BG RC
FLASHY
END
Press $\langle f 5\rangle$ for a full screen. Press the number keys. Press nonnumber keys.

Change FLASHY so that pressing 1 turns the screen black, 2 turns it white, 3 turns it red, etc.

TO FLASHY
2. Define VOWEL and run it.

TO VOWEL
PR [PRESS A VOWEL KEY]
MAKE "ANS RC
IF MEMBER? :ANS "AEIOU PR [RIGHT] ELSE PR [WRONG] PR [ ]
END
Instead of a list of vowels, type in a secret word. Let a friend guess your word by trying different letters.

Using RC stops the action until a key is pressed. RC? checks whether a key is being pressed. If no key is being pressed, the procedure continues.
3. Edit MASTER. Insert a new second line.

```
TO MASTER :T
IF RC? BG RC
IF :T < 10 STOP
etc.
```

Run MASTER 100; press number keys while it's running.
4. The test

## IF RC? BG RC

can be put inside a REPEAT.
Try this.
REPEAT 100 [FD 40 RT 117 IF RC? BG RC]
Then change another one of your procedures to allow you control over the background color while it's running.


## Lesson 30 Solid Shapes

Imagine the turtle drawing a box or something, but everytime it goes forward a step, it then hops to the lower left-hand corner and back, leaving a trail.


The result will be a solid shape.
The procedure SFD (for solid forward) will make the turtle move forward a step-hop to a fixed point and then hop back. When we draw the box, we'll use SFD :N instead of FD :N.

Before drawing the box, the coordinates of the fixed point :XF and :YF, must be defined. SFD will define :XT and :YT, the current point on the line being drawn. The turtle will move FD a step, hop to (:XF,:YF), hop back to (:XT,:YT).

1. Here's the procedure for SFD:
```
TO SFD :N
IF :N = © STOP
FD }
MAKE "XT XCOR
MAKE "YT YCOR
SETXY :XF :YF
SETXY :XT :YT
MAKE "N :N-1
SFD :N
END
```

A procedure to draw a solid green box of side :S is:
TO SBOX :S
MAKE "XF XCOR
MAKE "YF YCOR
PC 5
REPEAT 4 [SFD :S RT 90]
END
Try SBOX 40. Change SBOX to hide the turtle while coloring in the box.

Define a new set of procedures to draw solid shapes.
STR
SCIR
SPATTERN
SREC-to draw a solid rectangle of given height and width.

Make both the size and the pen color an input in your procedures.

TO STR :SIDE :C

TO SPATTERN :S :A :C

TO SCIR :DIAM :C

## TO SREC :H :W :C

Draw a picture using different solid shapes-maybe a locomotive. Write your procedures here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 31

## Flags

Define a procedure to draw a solid-color rectangle. Inputs should be the width, height, and color of the rectangle.

TO SREC :H :W :C
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Use SREC and your other solid procedures to draw a flag from each group.

1. Group 1

ITALY

$\qquad$

FRANCE

| BLUE |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |
|  | WHITE |  |
|  |  |  |
|  |  |  |
|  |  |  |

CHAD

2. Group 2

MADAGASCAR

|  | RED |
| :---: | :---: |
| WHITE |  |
|  | GREEN |

COLOMBIA

| YELLOW |  |
| :---: | :---: |
| BLUE |  |
| RED |  |

UNITED ARAB
EMIRATES

| RED | GREEN |
| :---: | :---: |
|  | WHITE |
|  | BLUE |
|  |  |

3. Group 3

## JAPAN


$\qquad$
$\qquad$

## LAOS

(RES
$\qquad$
$\qquad$

SWITZERLAND


## TONGA


$\qquad$
$\qquad$
4. Group 4

## BAHAMAS


$\qquad$

CZECHOSLOVAKIA


DENMARK



## Lesson 32 Fancy Forwards

SFD from Lesson 29 was a replacement for FD. You can define other types of FORWARDs, other ways to move from A to B.

Here are some examples:


Call them:

PF

Where,
PFD stands for pointed forward.
BFD stands for box forward.
JFD stands for jog forward.
If the distance from $A$ to $B$ is $: N$, the length of each segment of PFD and BFD is :N/3. JFD is more complicated.

Write a procedure for each of the new forward paths.
TO PFD :N
FD : N/3
RT 60
FD :N/3
LT 120
FD :N/3
RT 60
FD : N/3
END

TO BFD :N

## TO JFD :N

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Test each procedure: use PFD 50, etc.

Use each type of forward in drawing a box, a triangle with right turns, a triangle with left turns. Copy the results here.



Experiment:
Use the new forwards to draw other shapes-octagons, hexagons, etc.

Record the procedures and results.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 33

Fractals

To create a fractal, start with a fancy forward, such as BFD.

TO BFD :N
FD : N/3
RT 90
FD :N/3
LT 90
FD : N/3
LT 90
FD : N/3
RT 90
FD : N/3
END

Change all the FD :N/3 commands to BFD :N/3. Try BFD 80 What happens?

At some point we must stop being fancy and just draw a line. Insert, at the beginning, the test:
IF : N < 30 FD :N STOP

Try BFD 80. Copy the picture.

Change the 30 to 20 , then to 10 . Each time run BFD 80 and copy the picture.


Make fractals with PFD and JFD. Copy the results for : $\mathrm{N}<30$, :N < 20, : $\mathrm{N}<10$.


Design another fancy forward and turn it into a fractal.


## Lesson 34 <br> Snowflakes

This time, we'll use the fractal PFD in TR :SIDE. You'll have to redefine TR; call it SNOWFL.

TO SNOWFL :SIDE
REPEAT 3 [RT 120 PFD :SIDE]
END
Try SNOWFL 80 with different stopping sizes in PFD.
Use : $\mathrm{N}<30$, : $\mathrm{N}<10$, : $\mathrm{N}<5$.
Copy the pictures here. (At least the first two.)


Change the turn in SNOWFL to LT 120. Do another sequence of snowflakes. Copy them here.


Try using HEX instead of TR to generate snowflakes. Use both LT and RT.

Try the other fractals with TR and HEX. Copy at least three different snowflakes-state which fractal and which shape produced them.
$\qquad$
$\qquad$
$\qquad$

$169$


## Lesson 35 <br> Outputs

In advanced LOGO programs, you sometimes want to calculate something, but not print the calculated value.

A good example of this is the absolute value of a number. LOGO doesn't have an ABS function; however it's easy to write one. We want:

ABS : $X$ to be $\quad\left\{\begin{array}{l}: X \text { if }: X>0 \\ -: X \text { otherwise }\end{array}\right.$
To have ABS :X computed, but not necessarily printed, use OUTPUT.

TO ABS :X
IF :X > © OUTPUT :X ELSE OUTPUT - : X
END
OUTPUT can be written OP

IF :X > © OP :X ELSE OP -: X
END
Define ABS, then try ABS -6.
Copy what LOGO printed:
Now try IF ABS $-6<10$ PR [HAPPY]
What happened this time? $\qquad$
Write each of the following LOGO procedures:

1. SGN :X outputs +1 if $: X>0$
(1) if : $X=\mathbb{0}$
-1 if $: x<\mathbb{D}$
SGN is known as the sign function.
TO SGN :X
$\qquad$
$\qquad$
$\qquad$
2. $A V: X: Y$ outputs the average of $: X$ and $: Y$.

TO AV :X :Y
3. MAX :X : $Y$ outputs the larger of $: X$ and $: Y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
4. $\mathrm{MIN}: \mathrm{X}: \mathrm{Y}$ outputs the smaller of $: X$ and $: Y$.
$\qquad$
$\qquad$
$\qquad$
5. DIST :X1 :Y1 :X2 :Y2 outputs the square root of $(\mathrm{X} 1-\mathrm{X} 2)^{2}$ $+(Y 1-Y 2)^{2}$.

LOGO has a command SQRT; SQRT : $X$ outputs $\sqrt{: X}$
TO DIST :X1 :Y1 :X2 :Y2


## Lesson 36 Mirror Images

In this lesson, you'll make the turtle move in front of a mirror. To do this, you'll need a new procedure MFD (mirror forward).

If the mirror goes across the middle of the screen, the image of $(\mathrm{X}, \mathrm{Y})$ is $(\mathrm{X},-\mathrm{Y})$.


First draw a line across the middle of the screen. Return the turtle to the center with HOME.

Every time the turtle receives a MFD :N command, it should:

- Make a note of where it is; :XOLD :YOLD use MAKE "XOLD XCOR MAKE "YOLD YCOR.
- Move FD :N.
- Make a note of where it is now; :XNEW :YNEW.
- Hide the turtle, pen up.
- SETXY to image of old point.
- Pen down.
- SETXY to image of new point.
- Pen up, hop back to new point.
- Pen down, show turtle.

Write the procedure, MFD.
TO MFD : N

In these pictures, only the turtle's path is shown.

1. Use MFD, RT, LT, and FD (to lift the pen), to move the turtle along the path, drawing the reflections as well.
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$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

2. Change MFD to VMF (vertical mirror forward). This mirror goes up and down through the middle of the screen.


Move the turtle along these paths.
Your procedure should draw the reflections, too.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
3. If the mirror goes from lower left to upper right, the image of ( $\mathrm{X}, \mathrm{Y}$ ) is ( $\mathrm{Y}, \mathrm{X}$ ). Let DMF (diagonal mirror forward) be the procedure which reflects movement in this mirror.

> TO DMF :N


Use DMF to complete these pictures.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
$\qquad$
4. What happens when CMF, (combined mirror forward), is used? CMF : N should do all three reflections:

TO CMF :N
move FD : N from A to B
draw $\mathrm{A}^{\prime} \mathrm{B}^{\prime}$
draw $\mathrm{A}^{\prime \prime} \mathrm{B}^{\prime \prime}$
draw $A^{\prime \prime \prime} B^{\prime \prime \prime}$
hop back to B
$\qquad$
$\qquad$
$\qquad$
$\qquad$



## Lesson 37 Turtle Billiards

## You'll need ABS.

When this procedure is completed, you'll be able to:

- Tell LOGO the size of a rectangle (width :W and length :L).
- Have the rectangle appear on the screen.
- Have the turtle start at the lower right corner of the table with a heading of 315 (same as -45 ).
- Have the turtle proceed in a straight line; when it hits the edge of the table, it will bounce off the edge of the table like a billiard ball.


Break this project up into parts:

1. Draw the table, centered on the screen. Use SETXY, SETX, SETY. The lower right-hand corner is at :W/2 - :L/2
2. Place, aim, and start the turtle moving. Move 5 units at a time.
3. Check if so, $A B S: X C O R>: W / 2$. If so, change heading to -HEADING.

4. Check if ABS :YCOR > :L/2. If so, change heading to $180-$ HEADING.

5. Move the turtle again.

Write the procedure BILLIARDS.
TO BILLIARDS :L :W

## Optional Exercises

When BILLIARDS is working, change it to POOL. The turtle will stop when it reaches a corner. ("Reaches" means gets very close.)

Investigate which corner the turtle reaches on the different tables below. Use UR for upper right, LL for lower left, etc.

TO POOL :L :W

| Table <br> Length | 80 | 120 | 80 | 100 | 110 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| able <br> Width | 40 | 40 | 60 | 40 | 50 |
| Final <br> Corner |  |  |  |  |  |



## Lesson 38 Words

When LOGO sees BOX, HOUSE, etc., it assumes these are the names of procedures. To tell LOGO that a word is intended, you use "BOX "HOUSE.

LOGO can do a lot of things with words. To see some of them, enter and run DEMO.

1. Write down next to each PR what it produces.

TO DEMO
MAKE "W "ELEPHANTS
PR :W
PR COUNT :W
PR FIRST :W
PR BF:W
PR LAST :W
PR BL :W

PR [ ]
PR ITEM 4 :W
PR MEMBER? "H :W
PR MEMBER? "Z :W
END
If "ELEPHANTS were changed to "ZEBRAS, what would DEMO do? Write your guess here. Then change DEMO and run it.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
2. To indicate a word with no letters at all, use ". A word with no letters is called a null word. It's used mainly in tests.

The procedure DROP chops off one letter at a time.

> TO DROP :W

IF :W = " STOP
PR :W
MAKE "W BF :W
DROP :W
END

To use DROP, type DROP "THERE

Change DROP to drop the last letter each time. Write your procedure here.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Write a procedure CHOP that drops the first and last letter each time. Try CHOP "TIGERS then CHOP "ELEPHANTS.

TO CHOP :W

Put in another test so that CHOP works on words with any number of letters. (Using COUNT is one possibility.) Record your final CHOP here.
4. Write a procedure to print the letters of a word in a column.

TO COL :W


## Lesson 39 <br> Gluing Words

LOGO uses WORD to glue together two words to make a new one. To glue more than two words, use parentheses.

1. Run GLUE to see how it works. Write down what is printed.
```
TO GLUE
MAKE "W "BUTTER
MAKE "T "FLY
MAKE "P WORD :W :T
PR :P
MAKE "Q WORD :T "AWAY
PR :Q
MAKE "Z (WORD :W :T :Q)
PR :Z
END
```

2. Write ECHO, which doubles the word and prints the new word.

TO ECHO :W
MAKE "W $\qquad$

Try ECHO "THUMP
Make ECHO call itself; add ECHO :W as a last line. Then try ECHO "A.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Change ECHO so that, instead of printing : W , it prints the number of characters in $: W$. How long can $: W$ get before LOGO can't hold any more?
4. Write a procedure, CYCLE, to remove the first letter from a word and glue it onto the end. If you run CYCLE "SHARE, the result should be HARES.

TO CYCLE :W
5. Finally, write a pig latin translator. You enter a word:

If the word begins with a vowel, add WAY to the end.
If the word doesn't begin with a vowel, transfer the first letter to the end of the word. Keep this up until you get a word starting with a vowel. Then, add AY to the end.

You can assume there are, at most, four consonants at the beginning of any word.

TO PIG :W


## Lesson 40 More Words

These problems are more complicated. They involve all the word functions as well as REPEAT and, perhaps, recursion. There are several ways to do each one.

1. Write a procedure REV which takes a word :W and reverses the letters to form a new word. Call the new word :RW.

Hint: : RW begins with LAST :W
Its next letter is LAST of something else. Keep building up :RW. (How many letters will it have?)

[^0]Try REV "123456789. Does it work for numbers?
$\qquad$
$\qquad$
$\qquad$
A word which is the same read forward or backward is called a palindrome. Change REV to print PALINDROME, if the word was one.
2. Write a procedure DOUBLE to check whether a word has a double letter. $D O U B L E$ should print TRUE if there is a double letter, FALSE otherwise.

Hint: Look at FIRST :W and FIRST BF :W Are they the same?
Replace :W with BF :W and look again.

TO DOUBLE :W
3. Write a procedure INFO which tells how many consonants and how many vowels a word has.

You'll need to use IF MEMBER?; see Lesson 29.
TO INFO :W
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 41 Lists

LOGO can handle lists as well as separate words. A word begins with " and ends with a space. A list begins with [ and ends with ].

COUNT, ITEM, FIRST, LAST BF, BL all work with lists.

1. Run TRYLIST.

TO TRYLIST
MAKE "L [A BLUE FLY WAS BITING AT THE DOG ONCE]
PR :L
PR COUNT :L
PR ITEM 2 :L
END

Change TRYLIST so that every other word in the list, starting with word 2, is printed. (Use REPEAT.)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Change TRYLIST so that every third word, starting with word 3 , is printed.
2. Write BABBLE, a procedure in which:
: N is a list of nouns, for example, [DOGS CATS MICE ELEPHANTS]
:V is a list of verbs, for example, [LIKE FEAR CHASE]
:BABBLE prints a random item from : N , followed by a random item from V , followed by another random item from : N .
3. The elements of a list can also be lists. Change BABBLE so that : V looks something like:

MAKE "V [[ARE AFRAID OF] CHASE [CAN'T STAND]]
Make it more interesting. Change $: N$, too.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
4. Write MENU which contains:

- A list of appetizers. :A
- A list of main dishes. :MD
- A list of vegetables. :V
- A list of desserts. :D

MENU should select a random item from each list.
If you want the chance of skipping vegetables, let one of the items in $: V$ be [], the empty list.


## Lesson 42 <br> Gluing Lists

Two lists can be glued together in different ways.
SE (SENTENCE) makes one big list of the words in both lists. LIST makes a list whose items are the original lists.

## 1. Run DEMOLIST.

```
TO DEMOLIST
MAKE "A [DOGS CATS MICE]
MAKE "B [HOUSES TREES BIRDS]
MAKE "C LIST :A :B
PR :C
PR ITEM 2 :C
MAKE "D SE :A :B
PR :D
PR ITEM 2 :D
END
```

For getting at individual words, use SE.
2. Try to write a procedure DEVOWEL which removes all the vowels from the words of a list.
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$\qquad$
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$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Write TALKBACK which prints the words of a sentence in reverse order.

TO TALKBACK
4. Combine TALKBACK with REV, from Lesson 40, which reverses a word, to define a procedure which prints a list completely backward.

Try your procedure on: ABLE WAS I ERE I SAW ELBA and MADAM I'M ADAM.


## Lesson 43 <br> Tell LOGO Something

You can tell LOGO to wait until something is typed and 〈return〉 is pressed. RQ (REQUEST) does this.
$R Q$ is the list that was entered.

## 1. Try LOGIC.

TO LOGIC<br>PR [WHAT'S YOUR FULL NAME?]<br>MAKE "NAME RQ<br>PR [WHAT'S YOUR FAVORITE COLOR?]<br>MAKE "COL RQ<br>PR (SE :NAME [LIKES] :COL)<br>END

When SE is used with more than two lists or words, enclose the whole thing in parentheses. Write another logic-type program.
$\qquad$
$\qquad$
$\qquad$
2. Even a one-word answer is a list. To turn it into a word, use FIRST RQ.

Finish ANIMAL to include animals from the other continents.

```
TO ANIMAL
PR [TELL ME AN ANIMAL]
MAKE "AN FIRST RQ
IF MEMBER? :AN [LION ELEPHANT HYENA] PR [AFRICA]
IF MEMBER? :AN [KANGAROO BANDICOOT] PR [AUSTRALIA]
```

3. Write QUIZ. It should follow this outline:

- TO QUIZ :ANIM.
- Print TELL ME AN ANIMAL I DON'T KNOW.
- Change the animal entered by the player (remember! it's a list) to a word, :GUESS.
- Check if :GUESS is a member of :ANIM if yes, print ALREADY KNOWN; QUIZ :ANIM if no, use SE to add :GUESS to :ANIM, say thanks and call :QUIZ :ANIM.

To start the list, use QUIZ [].
4. Do another quiz. This time ask for names of tennis players or rock groups. Use LIST to build up the known players or groups. Don't change RQ to a word.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


Numbers also have to be changed from lists to words.

1. Write a simple addition quiz. Follow this outline:

- Let LOGO pick two numbers at random, say :A and :B.
- Print $3+4=$ ? (use the values of : $A$ and : $B$ )
- Change the answer to a word. Check if it's correct.
- Print RIGHT or WRONG. If wrong, tell the answer.

2. Fix up the quiz so the user gets three tries.

Use REPEAT 3 [............................ IF ....... PR [OK] STOP]
Print the answer if three mistakes are made.
3. Write GAME. LOGO picks a number from 1 to 100 . The player gets seven guesses; the player should be told whether each guess is TOO HIGH or TOO LOW.

Have the turtle draw a fancy star when the number is guessed.
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$\qquad$
$\qquad$
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$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Lesson 45 Testing

There are times when IF ..... ..... ELSE ..... is hard to use, especially if the actions are complicated or lengthy.

Another way is to use the commands: TEST

1. Try this.

> TO SIZE :N

TEST :N > 1000
IFT PR [A LARGE NUMBER]
IFF PR [NOT SO LARGE]
END

Try SIZE 100 and SIZE 9999.

Change SIZE so that SIZE 100 prints:

## 100 IS NOT SO LARGE

and SIZE 9999 prints:

## 9999 IS A LARGE NUMBER

2. Use TEST, IFT, IFF to write a game ANIMAL. Player is to guess an animal. If the guess is HORSE then print CORRECT. If the guess is not HORSE print THAT'S NOT IT.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
When ANIMAL is working, change it so the player gets 10 guesses. Write the complete game here.
3. What's being TESTed must be TRUE or FALSE. But the test can be a procedure which outputs TRUE or FALSE.

Try this:
TO SECRET :W
TEST RULE :W
IFT PR [YES]
IFF PR [NO]
END
TO RULE :W
IF MEMBER? "E :W OP "TRUE ELSE OP "FALSE END

SECRET prints YES if the word has an E, and prints NO if it doesn't.

Change RULE to check for double-letters (see Lesson 40).
4. If RULE is to check that :W has both an $E$ and an $R$, use ALLOF.

IF ALLOF MEMBER? "E :W MEMBER? "R :W OP "TRUE ELSE ...
To check for either an E or R , use ANYOF.

## IF ANYOF

ALLOF means both of two possibilities. ANYOF means either of two possibilities.

Write a secret rule game:

- LOGO asks for a word.
- Player enters a word.
- LOGO responds with YES or NO.
- LOGO asks for another word.
- Player keeps trying words until sure of the rule.

Make up your own rule for YES and NO.
TO GAME


## Lesson 46 Search and Replace

Suppose you wrote a story about a dog, and then decided that you wanted to change DOG to CAT everywhere in the story.

LOGO can look at the words of the list and make a replacement. It looks at the first word, decides whether or not to change it, then looks at the first word of BUTFIRST of the list.

Here's how to do it:

TO REPLACE :OLD :NEW :L
IF :L = [] OP []
TEST :OLD = FIRST :L
IFT OP SE :NEW REPLACE :OLD :NEW BF :L
IFF OP SE FIRST :L REPLACE :OLD :NEW BF :L END

Try REPLACE "DOG "CAT [THE DOG LOOKED LIKE MY DOG]

1. Write WORDPLACE to replace a letter within a word. TO WORDPLACE :OLD :NEW :W

Try WORDPLACE "T "B [TRITE]
2. You can make LOGO think THE QUICK BROWN DOG is a word. Use an apostrophe before and after the "word."

TO WORDDEMO
MAKE "W "'THE QUICK BROWN FOX'
PR :W
PR FIRST :W
END
To enter a sentence as a word, you also use apostrophes.
TO TELLME
PR [TYPE A SENTENCE]
MAKE "W FIRST RQ
PR :W
PR FIRST :W
END

Run TELLME. When TYPE A SENTENCE appears, type: 'THE QUICK BROWN FOX'

Write LISPER which changes every S to TH. Try LISPER with:

SISTER SUSIE SITTING ON A SOFA.
3. Use WORDPLACE in a decoding program. After the user types in the coded message, the procedure should print the message.
(Use apostrophes to enter the message as a word.)
Then LOGO should print CHANGE? (user types a letter) TO (user types a new letter)

The message should be changed and printed out.
LOGO should ask for the next change.
Try your decoder on this message:
ERY GZQT VABACGTF LGT OZCL XIRSOTH AB LGT ORNR JRIWSRRW.

## APPENDIX 1 <br> Comments About Editing Procedures

Making changes in a procedure, even correcting typographical errors, can be difficult at first. These observations may help.

1. Typing characters inserts them where the cursor is.
2. Pressing the delete key erases the character to the left of the cursor.

If your line reads
FD 250 RT 90
and you want it to read
FD 25 RT 90
Move the cursor to the space after 250 and press $\langle$ del $\rangle$.
3. CTRL K erases everything to the right of the cursor.
4. 〈Return〉 moves everything to the right of the cursor to the next line.
5. Press RUN/STOP or CTRL C to save a procedure.

## APPENDIX 2 <br> Formatting a Disk Saving and Reading Files

If you wish to save your LOGO procedures，you＇ll need a formatted disk．

Before loading LOGO，insert a blank disk in the drive and type：
OPEN 15，8， 15 〈return〉
PRINT\＃15，＂N0：LOGOFILES，MW＂〈return〉
（use your initials instead of MW）
The disk drive will make noises for about two minutes as the disk is formatted．

When the red light goes off，remove the disk，and label it．
Now load LOGO and proceed with your work．
At the end of your session，to see the names of all the procedures you have defined，type：

```
POTS <return>
(POTS stands for print out-titles)
```

To save all your procedures，pick a file name that means something to you，say，MWSHAPES．

Type：
SAVE＂MWSHAPES 〈return〉
The drive will make noises as the file is saved．

To read these procedures in the next time you use LOGO，first start up the LOGO program．When it is running，type：

READ＂MWSHAPES 〈return〉
When the file has been read，type：

## POTS

to see what procedures you have．
Each time you write a file，use a different file name．If you＇ve forgotten what you called a file，type：

CATALOG 〈return〉
to see the names of everything on the disk．

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Mary Jean Winter is a professor of Mathematics at Michigan State University. She has been actively involved in mathematics education (K-12) for the last 8 years. She was formerly a numerical analyst in industry and academia. She is the author of The Computer Playground series and Compumath Magic published by DATAMOST, Inc. She has also written Chivalry, Great Adventure, Wordspot and Witchnumber, published by Comm*Data; numerous articles on using calculators and computers in the classroom, as well as calculator activities for Scott Foresman's elementary series math textbook. The author also teaches computing at MSU Summer Computer Camps for children ages 10-16. She has a Ph.D. in mathematics from Carnegic Mellon University and an A.B. in mathematics and history from Vassar College.

## THE COMMODORE 64

## LIEI MIIR:11K

DATAMOST proudly introduces THE COMMODORE 64 LOGO WORKBOOK, the third in a series of educational computer books written especially for young people in grades 2 through 6 . The first series, COMPUTER PLAYGROUND, introduced BASIC programming by means of graphics, games and words. The second, COMPUMATH MAGIC, showed those who already knew some BASIC how to use it to solve problems. Now comes THE COMMODORE 64 LOGO WORKBOOK, which introduces the LOGO language and teaches how LOGO can be used in problem-solving.

Written for children, this wonderful book shows them what a "turtle" is, what procedures are, how to use visual problem-solving, variables, geometry, and even recursion. Combined with the Commodore 64 LOGO package, this book becomes a powerful learning experience with the educational language.

Structured in lesson form, two-thirds of THE COMMODORE 64 LOGO WORKBOOK is directly concerned with graphic geometric lessons, providing immediate visual satisfaction and teaching about symmetry and the idea of a limit at the same time. Problem-solving skills are developed and applied at every level. The last third of THE WORKBOOK deals with sentences and words, with applications in the game category.



[^0]:    TO REV :W

